

## 2.1 Limits

Consider  $f(x) = \frac{x^2 - 4}{x + 4}$ . What observations can you make?

How can we describe what happens at  $x = -2$ ?

Find the Limit:  $\lim_{x \rightarrow -3} \frac{x + 3}{x^2 + x - 6}$

Finding limits Analytically:

Finding limits Graphically:

Finding limits Numerically:

## 2.1

Find each limit.

$$1. \lim_{x \rightarrow 2} (x^2 + 3x - 5) =$$

$$2. \lim_{x \rightarrow \pi} (\sin x \cos x) =$$

$$3. \lim_{x \rightarrow 4} \frac{x - 4}{x^2 - 16} =$$

Find the limit.

$$4. \lim_{x \rightarrow 0} \frac{\sin x}{x} =$$

$$5. \lim_{x \rightarrow 0} \frac{\sin x + x}{x} =$$

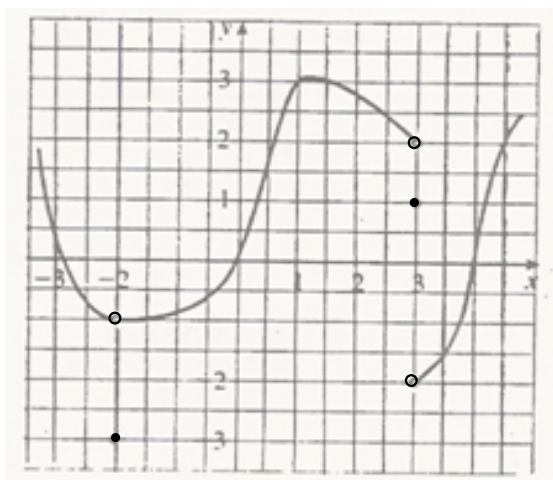
Left and right hand limits.

$$\lim_{x \rightarrow c^+} f(x) \qquad \lim_{x \rightarrow c^-} f(x)$$

Definition of a limit:

$$\lim_{x \rightarrow c} f(x) = L \quad \text{iff} \quad \lim_{x \rightarrow c^+} f(x) = \lim_{x \rightarrow c^-} f(x) = L$$

the limit doesn't necessarily equal the function!!!



(a)  $\lim_{x \rightarrow 1} f(x) =$       (b)  $\lim_{x \rightarrow 3^-} f(x) =$       (c)  $\lim_{x \rightarrow 3^+} f(x) =$

(d)  $\lim_{x \rightarrow 3} f(x) =$       (e)  $f(3) =$       (f)  $\lim_{x \rightarrow -2^-} f(x) =$

(g)  $\lim_{x \rightarrow -2^+} f(x) =$       (h)  $\lim_{x \rightarrow -2} f(x) =$       (i)  $f(-2) =$

## 2.1

Properties of Limits:

$$1. \lim_{x \rightarrow a} (f(x) + g(x)) = \lim_{x \rightarrow a} f(x) + \lim_{x \rightarrow a} g(x)$$

$$2. \lim_{x \rightarrow a} (f(x) \cdot g(x)) = \lim_{x \rightarrow a} f(x) \cdot \lim_{x \rightarrow a} g(x)$$

Given that  $\lim_{x \rightarrow a} f(x) = -3$ ,  $\lim_{x \rightarrow a} g(x) = 0$ ,  $\lim_{x \rightarrow a} h(x) = 8$ ,

find the limits that exist. If the limit does not exist, explain why.

$$(a) \lim_{x \rightarrow a} [f(x) + h(x)] = \quad (b) \lim_{x \rightarrow a} [f(x)]^2 =$$

$$(c) \lim_{x \rightarrow a} \sqrt[3]{h(x)} = \quad (d) \lim_{x \rightarrow a} \frac{1}{f(x)} =$$

$$(e) \lim_{x \rightarrow a} \frac{f(x)}{h(x)} = \quad (f) \lim_{x \rightarrow a} \frac{g(x)}{f(x)} =$$

$$(g) \lim_{x \rightarrow a} \frac{f(x)}{g(x)} = \quad (h) \lim_{x \rightarrow a} \frac{2f(x)}{h(x) - f(x)} =$$