### 2.3 Continuity

## How would you describe Continuity?

Where is $f(x)$ continuous?

## For what values of c does

$\lim _{x \rightarrow c} f(x)$ exist?


Where is the function discontinuous?

## Continuity at a point: (RS \#23)

$f(x)$ is continuous at $\mathrm{x}=\mathrm{c}$ if

1. $f(c)$ exists
2. $\lim _{x \rightarrow c} f(x)$ exists (remember this means left hand $=$ right hand)
3. $\lim _{x \rightarrow c} f(x)=f(c)$

3 types of discontinuities
hole (removable discontinuity)

1. jump:
2. removable:
3. infinite:

Find the values of $x$ where the graph is not continuous. Identify the type of discontinuity. Five reasons for your answers. (Use the continuity definition to justify)


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## Extended function-

## Continuous function-

${ }^{* * *}$ Compositions of continuous functions are continuous.***

## Intermediate Value Theorem (IVT)



