

3.7 Implicit Differentiation

Objectives:

- I can take the derivative by implicit differentiation

Consider $x^2 + y^2 = 9$ 1. Find the equation of the tangent line through $(2, -\sqrt{5})$

Steps for implicit differentiation

I. Take the derivative with respect to x II. Solve for $\frac{dy}{dx}$

For each of the following: A) find

B) Find the equation of the tangent and normal line at the given point

$$y^2 = x \quad (4, -2)$$

$$x^2 - y^2 = 25 \quad (-5, 0)$$

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$$\text{Find } \frac{dy}{dx} \quad x^2 = \frac{x^2+1}{y^2}$$

$$\text{Find } \frac{dy}{dx} \quad y^2 = \frac{x^2-1}{x^3}$$

$$\text{Find } \frac{dy}{dx} \quad x^2 + 2xy + y^2 = 0$$

$$\text{Find } \frac{d^2y}{dx^2} \quad y^2 = x^2 + 2x$$