

Let's try to approximate  $\sqrt{7}$  without a calculator

#### 4.5/4.2 Linearization, Differentials, and Antiderivatives

Objectives:

- I can find a general antiderivative
- I can evaluate using differentials
- I can find the linearization of a function

Use an appropriate linearization to approximate  $\sqrt{110}$

The linearization of  $f$  at  $a$  is given by:

$$L(x) = f'(a)(x - a) + f(a)$$

Find the linearization  $L(x)$  of  $f(x)$  at  $x=a$

$$f(x) = x + \frac{1}{x}, \quad a = 1$$

### Differentials

$\frac{dy}{dx}$  is a notation that represents the derivative.

Separately,  $dy$  and  $dx$  are called differentials.

Find  $dy$ . Then evaluate  $dy$  for the given values.

1.  $y = \frac{x}{x^2 - 1}, \quad x = 3, \quad dx = .01$

2.  $y = x\sqrt{x-1}, \quad x = 2, \quad dx = .005$

If  $f'(x) = 2x + 4$ , can we find  $f(x)$ ??

Find each general antiderivative

3.  $f'(x) = x^2 - 2x$       4.  $f'(x) = \sec^2 x$

5.  $f'(x) = \frac{1}{x+6}, x > -6$

Consider  $f'(x) = 2x + 4$  again. When finding  $f(x)$  what information would we need to find  $C$ ?

Find the particular antiderivative that passes through the point  $P$ .

6.  $f'(x) = 3x$      $P(1,5)$

$$7. f'(x) = \frac{1}{3x^3} \quad P(8,3)$$

$$8. f'(x) = x^2 + 2 + \sin x \quad P(0,5)$$