### 6.2.1 U-Substitution

Consider $f^{\prime}(x)=2 x \sin x^{2}$
What do you notice?

Can you find $f(x)$ ?

Integration by substitution (U-Substitution)

## $\int 2 x \sin x^{2} d x$

## Steps

1. Identify the inside function
2. Let $u=$ inside function
3. Find du
4. Get a "match" and substitute (If you can't get a "match" try another u)
5. Integrate
6. Use substitution to get your answer back in terms of $x$
7. Check by differentiating

Find each indefinite integral
$\int x e^{x^{2}} d x$
$\int x^{3} \cos \left(3 x^{4}\right) d x$

$$
\int e^{\cos x} \sin x d x \quad \int \sin ^{3} x \cos x d x
$$

$\int \sqrt{\sec x} \sec x \tan x d x \quad \int \frac{\ln ^{4} x}{2 x} d x \quad \int \tan x d x$

$$
\int \frac{\sqrt{\ln x}}{4 x} d x \quad \int \frac{d x}{x^{2}+16}
$$

$$
\int \frac{x}{x^{2}+1} d x
$$

