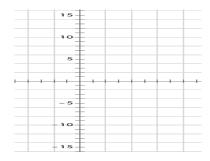
7.3.1 Solids of Revolution

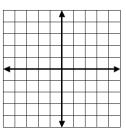
Consider the region bound by $f(x) = x^2$ and the x-axis over [0,4]



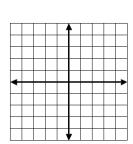
Rotate the region about the x-axis. We call this a solid of revolution. How could we find the volume of the solid?

Find the volume of the solid generated by rotating the enclosed region about the x-axis.

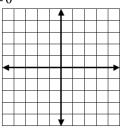
1.
$$y = \sqrt{x}$$
, $x = 4$, $y = 0$



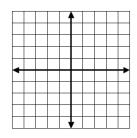
2.
$$y = \frac{1}{2}x$$
, $y = 0$, $x = 10$



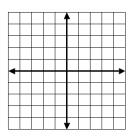
3.
$$y = e^x$$
, $x = 0$, $x = \ln 4$, $y = 0$



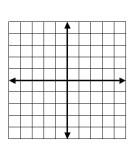
4.
$$y = \sqrt{4 - x^2}$$
, $y = 0$



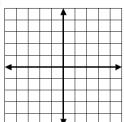
5.
$$y = \sin x$$
, $y = 0$ [0, π]



6.
$$y = x^2$$
, $y = x^3$

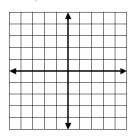


7.
$$y = \sin x$$
, $y = \sqrt{2} \left[\frac{\pi}{4}, \frac{3\pi}{4} \right]$

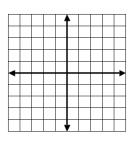


Find the volume of the solid generated by rotating the enclosed region about the y-axis.

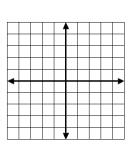
8.
$$y = x^2$$
, $x = 0$, $y = 4$



9.
$$y=2x$$
, $x=0$, $y=6$

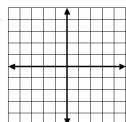


10.
$$y = x^2$$
, $x = 4$, $y = 0$

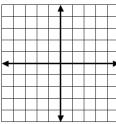


Find the volume of the solid generated by rotating the enclosed region about the given axis.

11.
$$y = x^3$$
, $y = \sqrt{x}$ about $y = 1$



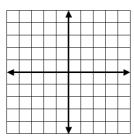
12.
$$y = x^3$$
, $y = \sqrt{x}$ about $y = -3$



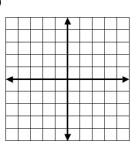
7.3.2 More Volumes

Find the volume of the solid formed by rotation the bounded region about the given axis.

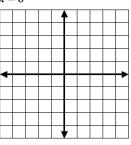
1.
$$y = x^2$$
, $x = 0$, $y = 4$, about $x = 0$



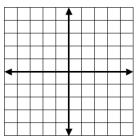
2.
$$y = 2x, x = 0, y = 6, about x = 0$$



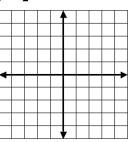
3.
$$y = x^2$$
, $x = 4$, $y = 0$, about $x = 0$



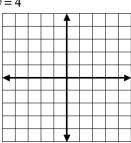
4.
$$y = \sqrt{x}$$
, $y = 0$, $x = 4$, about $x = -2$



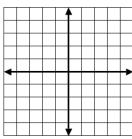
5.
$$y = x^2$$
, $y = 0$, $x = 2$, about $y = -2$



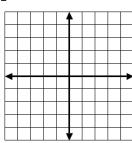
6.
$$y = x^2$$
, $y = 0$, $x = 2$, about $y = 4$



7.
$$y = x^2$$
, $y = 0$, $x = 2$, about $x = -1$



8.
$$y = x^3$$
, $y = \sqrt{x}$, about $y = 2$



9.
$$y = x^3$$
, $y = \sqrt{x}$, about $x = 1$

